# Extended 1. Number

Syllabus content	What do you kno	w?	R	Α	G	Comments
Types of numbers	<ul> <li>Identify and use:</li> <li>natural numbers</li> <li>integers (positive, zero and negative)</li> <li>prime numbers</li> <li>square numbers</li> <li>cube numbers</li> <li>common factors (eg HCF – highest cor</li> <li>common multiples (eg LCM – lowest conumbers)</li> <li>rational and irrational numbers</li> <li>reciprocals</li> </ul>	•				Surds HCF and LCM Rationalise the denominator
Sets	Understand and use set language, notation a  Definition of sets:  • $A = \{x: x \text{ is a natural number}\}$ • $B = \{(x, y): y = mx + c\}$ • $C = \{x: a \le x \le b\}$ • $D = \{a, b, c,\}$	nd Venn diagrams				
	<ul> <li>Notation:</li> <li>Number of elements in set A</li> <li>" is an element of"</li> <li>" is not an element of"</li> <li>Complement of set A</li> <li>The empty set</li> <li>Universal set</li> <li>A is a subset of B</li> <li>A is not a subset of B</li> <li>Union of A and B</li> <li>Intersection of A and B</li> </ul>	$n(A)$ $\in$ $\notin$ $A'$ $\emptyset$ $E$ $A \subseteq B$ $A \nsubseteq B$ $A \cap B$				

Syllabus content	What do you know?	R	Α	G	Comments
Powers and roots	Calculate with the following:				
	• squares	ш			
	square roots				
	• cubes				
	• cube roots				
	other powers and roots of numbers				
Fractions, decimals and percentages	Use the language and notation of the following in appropriate contexts:  • proper fractions				
	improper fractions				
	mixed numbers				
	decimals				
	percentages				
	Recognise equivalence and convert between these forms				
Ordering	Order quantities by magnitude and demonstrate familiarity with the symbols =, $\neq$ , >, < , $\geqslant$ and $\leqslant$				
The four operations	Use the four operations for calculations with:  • integers				Operations with
	• fractions				fractions and
	decimals				converting recurring decimals
	<ul> <li>correct ordering of operations (BIDMAS) and use of brackets</li> </ul>				to fractions.
Indices I	Understand and use indices (positive, zero and negative integers)				
	Understand and use the rules of indices for:  • multiplication of indices, e.g. $2^{-3} \times 2^4$				
	<ul> <li>division of indices, e.g. 2<sup>3</sup> ÷ 2<sup>4</sup></li> </ul>				
	<ul> <li>index numbers raised to an index, e.g. (2<sup>3</sup>)<sup>2</sup></li> </ul>				
Standard Form	Use the standard form $A \times 10^{\rm n}$ where $n$ is a positive or negative integer and $1 \leqslant A < 10$				Standard Form
	Convert numbers into and out of standard form				
	Calculate with values in standard form				0

Syllabus content	What do you know?	R A G	Comments
Estimation	Round values to a specified degree of accuracy of:		
	significant figures		
	decimal places		
	Make estimates for calculations involving numbers, quantities and measurements		
	Round answers to a reasonable degree of accuracy in the context of a given problem		
Limits of accuracy	Give upper and lower bounds for data rounded to a specified accuracy		
	Find upper and lower bounds of the results of calculations which have used data rounded to a specified accuracy		
Ratio and proportion	Understand and use ratio and proportion to:		
	give ratios in their simplest form		
	divide a quantity in a given ratio		
	<ul> <li>use proportional reasoning and ratios in context, e.g. map scales, determine best value</li> </ul>		
Rates	Use common measures of rate, e.g. hourly rates of pay, exchange rates between currencies		
	Apply other measures of rate, e.g. pressure, density		
	Solve problems involving average speed, including recall of speed/distance/ time formula		
Percentages	Calculate a percentage of a quantity		
	Express one quantity as a percentage of another		
	Calculate percentage increase or decrease		
	Calculate with simple and compound interest, including recall of formulas		
	Calculate using reverse percentages		

Syllabus content	What do you know?	R	A G	Comments
Using a calculator	Use a calculator efficiently			
	Enter values appropriately on a calculator, e.g. 2 hours 30 minutes			
	Interpret the calculator display appropriately, e.g. in money 4.8 means \$4.80			
Time	Calculate with time: seconds (s), minutes (min), hours (h), days, weeks, months, years, including the relationship between units			
	Calculate times in terms of the 24-hour and 12-hour clock			
	Read     clocks     timetables			
Money	Calculate with money			
	Convert from one currency to another			
Exponential growth and decay	Use exponential growth and decay, e.g. depreciation, population change			
Surds	Understand and use surds, including simplifying expressions			Surds HCF and LCM Rationalise the denominator
	Rationalise the denominator			O * ***

## 2. Algebra and graphs

Syllabus content	What do you know?	R	Α	G	Comments
Introduction to algebra	Use letters to represent generalised numbers				
	Substitute numbers into expressions and formulas				

Algebra basics

Syllabus content	What do you know?	R	Α	G	Comments
Algebraic manipulation	Simplify expressions by collecting like terms				
	Expand products of algebraic expressions:	〒	一	一	
	• with a single bracket, e.g. $3x(2x-4y)$			_	
	• with a pair of brackets, e.g. $(3x + y)(x - 4y)$				
	• with more than two brackets, e.g. $(x-2)(x+3)(2x+1)$	_			
	Factorise by extracting common factors			Ш	
	Factorise expressions of the form:				Factorisation
	• $ax + bx + kay + kby$	ш	ш	ш	Complete the Square
	$\bullet  a^2x^2 - b^2y^2$				Algebraic Fractions
	• $a^2 + 2ab + b^2$				<b>⊙</b> %%**
	• $ax^2 + bx + c$				2000 to 1
	• $ax^3 + bx^2 + cx$				TARES .
	Complete the square for expressions in the form $ax^2 + bx + c$				0.34.4
Algebraic fractions	Manipulate algebraic fractions such as:			П	
	$\bullet  \frac{x}{3} + \frac{x-4}{2}$	_		_	
	• $\frac{2x}{3} + \frac{3(x-5)}{2}$				
	• $\frac{3a}{3} \times \frac{9a}{10}$				
	• $\frac{3a}{3} \div \frac{9a}{10}$				
	$ \frac{1}{x-2} \div \frac{x+1}{x-3} $				
	Factorise and simplify rational expressions such as $\frac{x^2 - 2x}{x^2 - 5x + 6}$				

Syllabus content	What do you know?	R	Α	G	Comments
Indices II	Understand and use indices:  • positive, zero, negative  • fractional				Indices
	Understand and use the rules of indices, e.g. to simplify:  • $3x^{-4} \times \frac{2}{3}x^{\frac{1}{2}}$ • $\frac{2}{5}x^{\frac{1}{2}} \div 2x^{-2}$ • $\left(\frac{2x^5}{3}\right)^3$				
Equations	Construct expressions, equations and formulas  Solve linear equations in one unknown				Factorisation Complete the Square Algebraic Fractions
	Solve fractional equations with:  • numerical denominators  • linear algebraic denominators  Solve simultaneous linear equations in two unknowns				
	Solve quadratic equations by:				Simultaneous equations  O
	Change the subject of formulas				C.m.svom

Rearranging formulae



Syllabus content	What do you know?	R	Α	G	Comments
Inequalities	Represent and interpret inequalities, including on a number line				Inequalities and regions in a plane
	Construct, solve and interpret linear inequalities				
	Represent and interpret linear inequalities in two variables graphically				
	List inequalities that define a given region				
Sequences	Continue a given number sequence or pattern				
	Recognise patterns in sequences, including the term-to-term rule				
	Recognise relationships between different sequences				
	linear sequences	ш	ш	ш	
	quadratic sequences				
	cubic sequences				
	exponential sequences				
	simple combinations of these				
	<ul> <li>Find and use the nth term of sequences</li> </ul>				
Proportion	Express direct proportion in algebraic terms				
	Express inverse proportion in algebraic terms				
	Use algebraic expressions of direct and indirect proportion to find unknown quantities				

Syllabus content	What do you know?	R	Α	G	Comments
Graphs in practical	Use and interpret graphs in practical situations including:				
situations	travel graphs	ш		ш	
	conversion graphs				
	Draw graphs from given data				
	Apply the idea of rate of change to simple kinematics involving:				
	distance–time graphs	Ш	ш	Ш	
	speed–time graphs				
	acceleration and deceleration				
	Calculate distance travelled as area under a speed–time graph				
Graphs of functions	Construct tables of values, and draw, recognise and interpret graphs for functions of the following forms:				
	• $ax^n$ (includes sums of no more than three of these) where $n=-2, -1, -\frac{1}{2}, 0, \frac{1}{2}, 1, 2, 3$ and a is a rational number				
	• $ab^x + c$ where $a$ and $c$ are rational numbers and $b$ is a positive integer				_
	Solve associated equations graphically, including finding and interpreting roots by graphical methods	Ш		Ш	
	Draw and interpret graphs representing exponential growth and decay problems				
Sketching curves	Recognise, sketch and interpret graphs of the following functions:  • linear				Curved graphs Quadratic (parabola)
	• quadratic				and finding gradients
	• cubic				by differentiation.
	reciprocal				
	exponential				© ACCOUNT
	(knowledge of turning points, roots, symmetry, vertical and horizontal asymptotes is required)				

Syllabus content	What do you know?	R	A G	Comments
Differentiation	Estimate gradients of curves by drawing tangents			
	Use the derivatives of functions of the form $ax^n$ , where a is a rational constant and n is a positive integer or zero, and simple sums of not more than three of these			
	Apply differentiation to gradients and stationary points (turning points)			
	Discriminate between maxima and minima by any method			
Functions	Understand functions, domain and range and use function notation			
	Understand and find inverse functions $f^{-1}(x)$			
	Form composite functions as defined by $gf(x) = g(f(x))$			

## 3. Coordinate geometry

Syllabus content	What do you know?	R	Α	G	Comments
Coordinates	Use and interpret Cartesian coordinates in two dimensions				
Drawing linear graphs	Draw straight-line graphs for linear equations				Linear Functions (Straight lines)
Gradient of linear graphs	Find the gradient of a straight line				213
	Calculate the gradient of a straight line from the coordinates of two points on it				0 3 3
Length and midpoint	Calculate the length of a line segment				
	Find the coordinates of the midpoint of a line segment				
Equations of linear graphs	Interpret and obtain the equation of a straight-line graph				

Syllabus content	What do you know?	R	Α	G	Comments
Parallel lines	Find the gradient and equation of a straight line parallel to a given line				
Perpendicular lines	Find the gradient and equation of a straight line perpendicular to a given line				

## 4. Geometry

Syllabus content	What do you know?	R A G	Comments
Geometrical terms	Use and interpret the following geometrical terms:		
	• point		
	• vertex		
	• line		
	• plane		
	• parallel		
	perpendicular		
	perpendicular bisector		
	bearing		
	right angle		
	<ul> <li>acute, obtuse and reflex angles</li> </ul>		
	<ul> <li>interior and exterior angles</li> </ul>		
	• similar		
	• congruent		
	scale factor		
	Use and interpret the vocabulary of:		
	<ul> <li>triangles</li> </ul>		
	special quadrilaterals		
	<ul> <li>polygons</li> </ul>		
	• nets		
	• solids		
	Use and interpret the vocabulary of a circle		

Syllabus content	What do you know?	R	Α	G	Comments
Geometrical constructions	Measure and draw lines and angles				
	Construct a triangle, given the lengths of all sides, using a ruler and pair of compasses only				
	Draw, use and interpret nets				
Scale drawings	Draw and interpret scale drawings				
	Use and interpret three-figure bearings				
Similarity	Calculate lengths of similar shapes				Similar Shapes
	Use the relationships between lengths and areas of similar shapes and lengths, surface areas and volumes of similar solids				
	Solve problems and give simple explanations involving similarity				0=349
Symmetry	Recognise line symmetry and order of rotational symmetry in two dimensions				
	Recognise symmetry properties of prisms, cylinders, pyramids and cones				
Angles	Calculate unknown angles and give simple explanations using the following geometrical properties:				
	<ul> <li>sum of angles at a point = 360°</li> </ul>				
	<ul> <li>sum of angles at a point on a straight line = 180°</li> </ul>				
	<ul> <li>vertically opposite angles are equal</li> </ul>				
	<ul> <li>angle sum of a triangle = 180°</li> </ul>				
	<ul> <li>angle sum of a quadrilateral = 360°</li> </ul>				
	Know and use angle properties of regular and irregular polygons				
	(you are expected to use the correct geometrical terminology when giving reasons for answers)				

Syllabus content	What do you know?	R	Α	G	Comments
Circle theorems I	Calculate unknown angles and give explanations using the following geometrical properties of circles:  angle in a semicircle = 90°  angle between tangent and radius = 90°  angle at the centre is twice the angle at the circumference  angles in the same segment are equal  opposite angles of a cyclic quadrilateral sum to 180° (supplementary)				
	alternate segment theorem				
	(you are expected to use these geometrical properties when giving reasons for answers)				
Circle theorems II	Use the following symmetry properties of circles:				

#### 5. Mensuration

Syllabus content	What do you know?	R A G	Comments
Units of measure	Use metric units of:		
	• mass		
	length		
	• area		
	volume		
	• capacity		
	in practical situations		
	Convert quantities into larger or smaller units		

Syllabus content	What do you know?	R	Α	G	Comments
Area and perimeter	Carry out calculations involving the perimeter and area of a:     rectangle     triangle     parallelogram				
	trapezium				
Circles, arcs and sectors	Carry out calculations involving the circumference and area of a circle				
	Carry out calculations involving arc length and sector area as fractions of the circumference and area of a circle				
Surface area and volume	Carry out calculations and solve problems involving the surface area and volume of a:				
Compound shapes and parts of shapes	Carry out calculations and solve problems involving perimeters and areas of:  compound shapes parts of shapes  Carry out calculations and solve problems involving surface areas and volumes of:  compound solids parts of solids				

## 6. Trigonometry

Syllabus content	What do you know?	R	Α	G	Comments
Pythagoras' theorem	Know and use Pythagoras' theorem				
Right-angled triangles	Know and use the sine, cosine and tangent ratios for acute angles in calculations involving sides and angles of a right-angled triangle				Trig ratios Sine rule
	Solve problems in two dimensions using Pythagoras' theorem and trigonometry				Cosine rule
	Know that the perpendicular distance from a point to a line is the shortest distance to the line				0 <b>3</b> 3 3 3
	Carry out calculations involving angles of elevation and depression				
Exact trigonometric values	Know the exact values of: • $\sin x$ for $x = 0^\circ$ , $30^\circ$ , $45^\circ$ , $60^\circ$ and $90^\circ$				
	<ul> <li>cos x for x = 0°, 30°, 45°, 60° and 90°</li> <li>tan x for x = 0°, 30°, 45° and 60°</li> </ul>				
Trigonometric functions	Recognise, sketch and interpret the following graphs for $0^{\circ} \leqslant x \leqslant 360^{\circ}$ :  • $y = \sin x$ • $y = \cos x$				
	• $y = \tan x$ Solve trigonometric equations involving $\sin x$ , $\cos x$ or $\tan x$ , for $0^{\circ} \le x \le 360^{\circ}$				
Non-right-angled triangles	Use the sine rule in calculations involving lengths and angles for any triangle				
	Use the cosine rule in calculations involving lengths and angles for any triangle				
	Use the formula area of triangle = $\frac{1}{2}ab \sin C$				
Pythagoras' theorem and trigonometry in 3D	Carry out calculations and solve problems in three dimensions using Pythagoras' theorem and trigonometry, including calculating the angle between a line and a plane				

#### 7. Transformations and vectors

Syllabus content	What do you know?	R A G	Comments
Transformations	<ul> <li>Recognise, describe and draw the following transformations:</li> <li>Reflection of a shape in a straight line</li> <li>Rotation of a shape about a centre through multiples of 90°</li> <li>Enlargement of a shape from a centre by a scale factor</li> <li>Translation of a shape by a vector (x y)</li> </ul>		
Vectors in two dimensions	Describe a translation using a vector represented by $\begin{pmatrix} x \\ y \end{pmatrix}$ , $\overrightarrow{AB}$ or a Add and subtract vectors  Multiply a vector by a scalar		
Magnitude of a vector	Calculate the magnitude of a vector $\begin{pmatrix} x \\ y \end{pmatrix}$ as $\sqrt{x^2 + y^2}$		
Vector geometry	Represent vectors by directed line segments  Use position vectors		
	Use the sum and difference of two or more vectors to express given vectors in terms of two coplanar vectors  Use vectors to reason and to solve geometric problems		

## 8. Probability

Syllabus content	What do you know?	R	Α	G	Comments
Introduction to probability	Understand and use the probability scale from 0 to 1				
	Understand and use probability notation				
	Calculate the probability of a single event				
	Understand that the probability of an event not occurring = 1 – the probability of the event occurring				
Relative and expected frequencies	Understand relative frequency as an estimate of probability				
	Calculate expected frequencies				
Probability of combined events	Calculate the probability of combined events using, where appropriate: <ul><li>sample space diagrams</li><li>Venn diagrams</li><li>tree diagrams</li></ul>				
Conditional probability	Calculate conditional probability using Venn diagrams, tree diagrams and tables				

### 9. Statistics

Syllabus content	What do you know?	R	Α	G	Comments
Classifying statistical data	Classify and tabulate statistical data				
Interpreting statistical data	Read, interpret and draw inferences from tables and statistical diagrams				
	Compare sets of data using tables, graphs and statistical measures				
	Appreciate restrictions on drawing conclusions from given data				

Syllabus content	What do you know?	R	Α	G	Comments
Averages and measures	Calculate the:				
of spread	• mean	ш		ш	
	median				
	• mode				
	• quartiles				
	• range				
	• interquartile range				
	for individual data and distinguish between the purposes for which these are used				
	Calculate an estimate of the mean for:				
	grouped discrete data	ш	ш	ш	
	grouped continuous data				
	Identify the modal class from a grouped frequency distribution	Ш		Ш	
Statistical charts and	Draw and interpret:				
diagrams	• bar charts				
	• pie charts				
	• pictograms				
	stem-and-leaf diagrams				
<b>a</b> ,, , , ,	simple frequency distributions				
Scatter diagrams	Draw and interpret scatter diagrams	Ш		Ш	
	Understand what is meant by positive, negative and zero correlation				
	Draw by eye, interpret and use a straight line of best fit				
Cumulative frequency diagrams	Draw and interpret cumulative frequency tables and diagrams				
	Estimate and interpret the median, percentiles, quartiles and interquartile range from cumulative frequency diagrams				
Histograms	Draw and interpret histograms				
	Calculate with frequency density				